

RELIABILITY BASED POWER DISTRIBUTION SYSTEMS PLANNING USING CREDIBILITY THEORY

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Abstract: This paper presents an analytical technique for distribution system planning based on reliability evaluation using credibility theory. With the development of economy and society power planning is facing with the influence of much uncertainty, which are mainly power distribution network. Power system especially at the distribution level is prone to failures and disturbances as many devices are responsible for the successful operation of a radial distribution system. We also mention whether the work has been done at the strategic level, i.e. if it concerns the planning of power distribution system based on reliability and uncertainty.

Keywords: Power Distribution system, Credibility Theory, Reliability evaluation.

I. INTRODUCTION

The increased demand of reliable power with which system are designed, power distribution company need for higher reliable and lower operational costs, are forcing companies to continuously search for ways to improve their performance. Reliability models decision support systems and uncertainty analysis tools are examples of approaches taken by system in a challenge to develop their operational performance and remain competitive in the threat of competition. Godfrey et al (1996) identified three major issues for the implementation of reliability planning. Reliability data Customer damage function data reliability analysis software to these have been added: Policy Business process Research Skills development. All of these aspects present challenges for distribution planners because of a history of no or only limited reliability assessments. Billinton et al (1984) and Ajodhia (2002) had been studied a lack of data on distribution system reliability and customer impact has forced planners to adopt deterministic approaches to system planning and, historically, redundancy-planning decisions have been based on simple rules. New requirements to assess the reliability constraints of reinforcement alternatives need quantitative reliability analysis as well as uncertainty to use the results for decision-making.

Khator et al (1997) developed a power distribution planning is a complex task in which planners must ensure that there is adequate substation capacity (transformer capacity) and feeder capacity (distribution capacity) to meet the load demands. Decisions such as allocation of power flow, installation of feeders and substations, and procurement of transformers are costly ones which must be evaluated carefully. The review of research problems as well as models related to the planning of substations and/or distribution feeders. Sagar et al (2013) described the concept and characteristics of smart grid distribution systems, basic difference between conventional and smart grid distribution systems, functional management and reliability evaluation of smart grid distribution systems. In smart grid distribution system, remotely controlled high rated power electronic switches were used in the place of normal disconnecting switches on feeder. In normal operation of distribution system, these act as normally closed switches. Firuzabad et al (2009) presented a preventive maintenance application-based study and modeling of failure rates in breakers of electrical distribution systems. They were considered as a part of a Reliability Centered Maintenance application program. A number of load point reliability indices were derived using the mathematical model of the failure rate, which is established using the observed data in a distribution

system. Lantharthong et al (2012) developed a reliability evaluation technique which was applied in distribution system planning studies and operation. Reliability evaluation of distribution systems has been the subject of many recent papers and the modeling and evaluation techniques had been improved considerably. J. Ramírez et al (2004) were presented a new possibilistic (fuzzy) model for the multiobjective optimal planning of power distribution networks that finds out the nondominated multiobjective solutions corresponding to the simultaneous optimization of the fuzzy economic cost, level of fuzzy reliability, and exposure (optimization of robustness) of such networks, using an original and powerful meta-heuristic algorithm based on Tabu Search. The model also allows determining the optimal reserve feeders that provided the best distribution network reliability at the lowest cost for a given level of robustness. The model had been intensively tested in real distribution networks, which proves their practical application to large power distribution systems. Billinton et al (2006) illustrated weather environment can severely impact the performance of an overhead distribution system and an electric utility's operational ability. The likelihood of system failure increases due to enhanced line failure rates during bad weather periods. Reliability appraisals without incorporating weather conditions can be quite optimistic and affect planning and design decisions. Recognition of various weather contributions to the total system performance indices help to pinpoint situations where investment may provide maximum reliability improvement. An approach was presented to assess distribution system reliability in different weather conditions such as normal, adverse and extreme and illustrated using a practical distribution system. Brown et al (1998) illustrated distribution system reliability assessment is able to predict the interruption profile of a distribution system based on system topology and component reliability data. Unfortunately, many utilities do not have enough historical component reliability data to perform such an assessment, and are not confident that other sources of data are representative of their particular system. These utilities do not incorporate distribution system reliability assessment into their design process and forego its significant advantages. He presented a way of gaining confidence in a reliability model by developing a validation method. This method automatically determines appropriate default component reliability data so that predicted reliability indices match historical values. The result was a validated base case from which incremental design improvements can be explored. Allan et al (1991) had been described an electrical distribution system for use in teaching power system reliability evaluation. It includes the entire main element found in practical system. However, it was sufficiently small that studied can analyses it using hand calculations and hence fully understand reliability models and evaluation techniques. The data needed to perform basic reliability analyses. It also contains the basic results for a range of case studied and alternative design/operating configurations. Nahman et al (2003) studied effects of uncertain input data on the performance evaluation of a distribution system are analyzed. A criterion was introduced for assessing the grade of uncertainty of the results obtained in the calculation of maximum loads, voltage drops, energy losses, and characteristic reliability indices of a network if some input parameters are only guesses based on limited experience, measurements, and/or statistical data. Reasonable outputs bounds are determined based upon the shape of the function measuring the uncertainty. High uncertainty of a result obtained indicates that a re-examination of relevant uncertain input data would be recommendable for a more precise quantification. The method proposed was applied to a real life example for illustration.

II. CREDIBILITY THEORY

Credibility Theory is the cornerstones of actuarial science as applied to evaluate power distribution system reliability. The word credibility was originally introduced into actuarial science as a measure of the credence that the actuary believes should be attached to a particular body of experience for rate making purposes. Thus we say that the loss experience under a new class of insurance is "still too small to be credible", implying that the experience which will develop in the future may well be very different from that so far collected, and also implying that we have more confidence in our prior knowledge based on other data such as current rates for similar classes. Again, the statement that the private passenger automobile liability experience in Pennsylvania is "fully credible for rate making", implies that the experience, after adjustment by trend factors, is adequate to establish the overall rate level in the state without reference to previous rates or data or to experience in other states. In many cases a body of data is too small to be fully credible but large enough to have some credibility. A scale of credibility has been established which gives 0 credibility to data too small to be any use for rate making and credibility to data which are fully credible.

A. Least squares credibility:

Suppose you have two independent estimates x and y of a quantity, with respective expected squared errors u and v . Take a weighted average

$$a = zx + (1 - z)y.$$

The expected squared error of 'a' is

$$w = z^2u + (1 + z)^2v.$$

for z minimizes w.

$$dw/dz = 2zu + 2(z - 1)v.$$

If you set that to zero you get: $zu + zv = v$, or $z = v/(u + v)$. Then $1 - z$ is $u/(u + v)$. This makes it look like each estimate gets a weight proportional to the expected squared error of the other. To express the weights as properties of the estimates themselves, note that $\frac{\frac{1}{u}}{\frac{1}{u} + \frac{1}{v}} = \frac{1}{1 + \frac{u}{v}} = \frac{v}{u + v} = z$. This shows that each estimate gets a weight proportional to the reciprocal of its expected squared error. Least squares credibility is an application of this principle.

B. Non Linear Estimation:

So far this discussion has been non-parametric. That is, the forms of the distributions have not entered in. That is the advantage of linear estimates with squared error penalties. If you have some information about the type of distribution available, you can give up the restriction to linear functions. In a Bayesian framework the class experience becomes the prior distribution for the member experience, and then the Bayesian conditional expected value of the member mean given the data is the least squares estimator of the member mean of any sort, linear or not. Feng et al (2008) in some cases the conditional mean is a linear function of the data (e.g., normal and gamma distributions) so the linear restriction of credibility theory does not reduce the accuracy. However in highly skewed distributions, like some lognormal cases, the Bayes estimate is highly non-linear, and credibility weighting can give large errors for classes with small means. If the distribution type is fairly well understood, Bayesian methods would be preferable in such cases. However, an alternative when the member means can be very different from each other is to do the usual credibility estimation in the logs of the data, then exponentiate the results. This introduces a downward bias, however, which has to be adjusted multiplicatively to balance to the overall data.

C. Credibility Measure of Fuzzy Event:

A few no stochastic but uncertain phenomena in power systems can be modeled as fuzzy variables. Let $(-)$ be a nonempty set, $P(-)$ the power set of $(-)$ and ξ is a fuzzy variable with the membership function $\mu_{\xi}(x)$. The possibility of a fuzzy event $A \in P(-)$ is defined as, $P\{A\} = \sup_{x \in A} \mu_{\xi}(x)$, where \sup is the supremum operator. The necessity measure Nec is defined as, $Nec\{A\} = 1 - Pos\{A^c\}$, where A^c is the complement. Obviously, Pos and Nec are one pair of dual measure Baoding et al(2002).

In order to give a self-dual measure for fuzzy events, a credibility measure Cr is defined as follows

It is easy to verify that $Cr\{A\} + Cr\{A^c\} = 1$. The fuzzy event must hold if its credibility is 1, and fail if its credibility is 0.

Theorem 1: Relationship between the credibility measure and membership function

Definition: Let ξ be a fuzzy variable; then the possibility, the necessity, and the credibility of the fuzzy event A are expressed as follows:

$$P\{A\} = \sup_{x \in A} \mu_{\xi}(x) \quad (2)$$

$$Nec\{A\} = 1 - \sup_{x \in A^c} \mu_{\xi}(x) \quad (3)$$

$$Cr\{A\} = \frac{1}{2} (Pos\{A\} + Nec\{A\}) \quad (4)$$

Where $\mu_{\xi}(x)$ is membership function of ξ .

In traditional fuzzy set theory, possibility measure is considered to be a parallel concept of probability measure. But it does not possess self-duality: when $Pos\{A\} = 1$, fuzzy event A is not always true; when $Nec\{A\} = 0$, A may also be true.

In order to solve this problem, Liu et al (2002). In this theory, credibility measure which corresponds to probability measure in probability theory possesses self-duality and monotonicity – when $\text{Cr} \{A\} = 1$, fuzzy event A is inevitably true; otherwise it is false.

III. MODELING OF FUZZY FACTORS

The component failure rate and repair time is normally used to measure the probability of failure and repair of a particular component. While component status in the future and repair is not predictable, the failure rate and repair time of such component can be obtained from historical data in addition to failure rate and repair time can be modeled by triangular fuzzy variable for failure rate is $\lambda = [\lambda_1, \lambda_2, \lambda_3]$ and fuzzy variable for repair time is $r = [r_1, r_2, r_3]$.

For failure rate

$$\mu_{\lambda}(x) = \begin{cases} 0 & \text{if } x < \lambda_1 \\ \frac{x - \lambda_1}{\lambda_2 - \lambda_1} & \text{if } \lambda_1 \leq x < \lambda_2 \\ \frac{\lambda_3 - x}{\lambda_3 - \lambda_2} & \text{if } \lambda_2 \leq x < \lambda_3 \\ 0 & \text{if } x \geq \lambda_3 \end{cases} \quad (5)$$

And repair time

$$\mu_r(x) = \begin{cases} 0 & \text{if } x < r_1 \\ \frac{x - r_1}{r_2 - r_1} & \text{if } r_1 \leq x < r_2 \\ \frac{r_3 - x}{r_3 - r_2} & \text{if } r_2 \leq x < r_3 \\ 0 & \text{if } x \geq r_3 \end{cases} \quad (6)$$

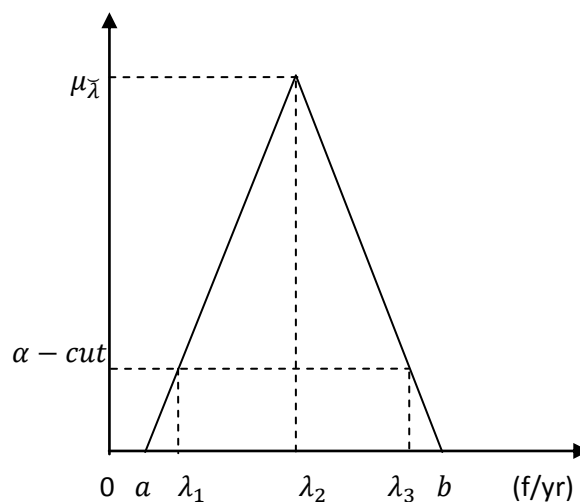


Fig. 1. Membership function of failure rate

The triangle membership function of failure rate & repair time can be easily created. The point estimate corresponds to 1.0 of the membership function grade. The significant level is always a small percentage such as 0.05 (5%). The half of α is located at each of the two bounds in the t-distribution. Conceptually, the significant level is somewhat similar to the fuzzy degree represented by the membership function grade since both of them reflect a subjective confidence. Therefore, it can be assumed that the lower and higher bounds obtained from (5&6) correspond to the two points (λ_1 and λ_3) in the membership function that has a membership grade of α (such as 0.1). With the three points of (λ_1, α), ($\lambda_2, 1$), and (λ_3, α), the two linear algebraic equations in the form of $y = a + bx$ can be built and the two end points ($a, 0$) and ($b, 0$) in the membership function can be calculated. When α is so small (0.025), a and λ_1 should be very close and so are b and λ_3 . In other words, it is also acceptable to directly use λ_1 and λ_3 as the two end points of the membership function.

IV. RELIABILITY INDICES

Power distribution systems are often radial and consist of series connections of components like lines, transformers, isolating switches, fuses, etc. This is important to evaluate the service continuity requires in between power resource and load to be online. Therefore, the effect of the series system failure rate $\tilde{\lambda}_s$ repair time \tilde{r}_s and time to failure (up time) \tilde{T}_s are taken into account with uncertainty as follows:

$$\tilde{\lambda}_s = \sum \tilde{\lambda}_i \quad (7)$$

$$\tilde{r}_s = \frac{\sum \tilde{\lambda}_i \tilde{r}_i}{\sum \tilde{\lambda}_i} \quad (8)$$

$$\tilde{T}_s = \frac{\tilde{\lambda}_s}{\tilde{\lambda}_s + 1/\tilde{r}_s} \approx \sum \tilde{\lambda}_i \tilde{r}_i \quad (9)$$

Where $\tilde{\lambda}_i$, \tilde{r}_i are failure rate and repair time of equipment i respectively. Subscript s expresses equivalent series network from power sending end to the receiving end. The reliability indices that have been evaluated they are not deterministic values but are the expected or average values of an underlying probability distribution and hence only represent the long-run average values. Similarly the word “average” or “expected” will be generally omitted from all other indices to be described, but again it should be noted that this adjective is always implicit in the use of these terms Billinton et al (1996). Things that failure rate of a distribution system component are usually assumed to be constant in conventional reliability evaluation of distribution system. It has been realised from the real-time operation that a component will experience more failures during heavy loading condition than those during light loading condition, which means that the failure rate of a component in real-time operation is not constant and varies with loading condition. In order to improve the reliability evaluation to the distribution system, uncertainty factors about failure rate considered under conventional reliability analysis of distribution system in the work. Although the three primary indices are fundamentally important, they do not always give a complete representation of the system behavior and response. For instance, the same indices would be evaluated irrespective of whether no customers were connected to the load point or whether the averages load at a load point. In order to reflect the severity or significance of a system outage, additional reliability indices can be and frequently are evaluated Billinton et al (1996). The additional indices that are most commonly used are defined in the following sections. The additional reliability indices with uncertainty are expresses as

- (i) System average interruption frequency index (SAIFI)

$$\text{SAIFI} = \frac{\text{total number of customer interruption}}{\text{total number of customer served}}$$

$$\text{SAIFI} = \frac{\sum \tilde{\lambda}_i N_i}{\sum N_i} \left(\frac{\text{int}}{\text{cus}} - \text{yr} \right) \quad (10)$$

Where N_i is the number of users on load point i .

- (ii) System Average Interruption Duration Index (SAIDI)

$$\text{SAIDI} = \frac{\text{sum of customer interruption duration}}{\text{total number of customers}}$$

$$\text{SAIDI} = \frac{\sum \tilde{T}_i N_i}{\sum N_i} \left(\frac{\text{hr}}{\text{cus}} - \text{yr} \right) \quad (11)$$

- (iii) Customer Average Interruption Duration Index (CAIDI)

$$\text{CAIDI} = \frac{\text{sum of customer interruption durations}}{\text{total number of customer interruptions}}$$

$$\text{CAIDI} = \frac{\sum \tilde{T}_i N_i}{\sum \tilde{\lambda}_i N_i} \left(\frac{\text{hr}}{\text{int}} \right) \quad (12)$$

Distribution system planning:

The distribution system of three feeders is used to demonstrate the feasibility of the proposed method. A signal line diagram of the distribution system is shown in Fig. 1. This distribution system contained three feeders F1, F2 and F3. The 12 load points are residential and commercial customer type. Feeder F1 contained 5 load points, feeder F2 contained 4 load points and feeder F3 contained 3 load points. The different four cases are considered for the system study. Case1- System with lateral protection, Case- 2: System with lateral protection and Disconnection, Case-3: System with load transfer and Case-4: System without protection. The input data are used for the study of distribution system reliability are shown in Table 1 and Table 2. Table 1 shows customer related data at different load points connected to number of customers and average load. Table 2 shows Line section length from L1 to L12 and disconnection length from D1 to D12, their failure rate in frequency per year for each feeder. The repair time for line section and disconnection is 4 hours and 2 hours respectively.

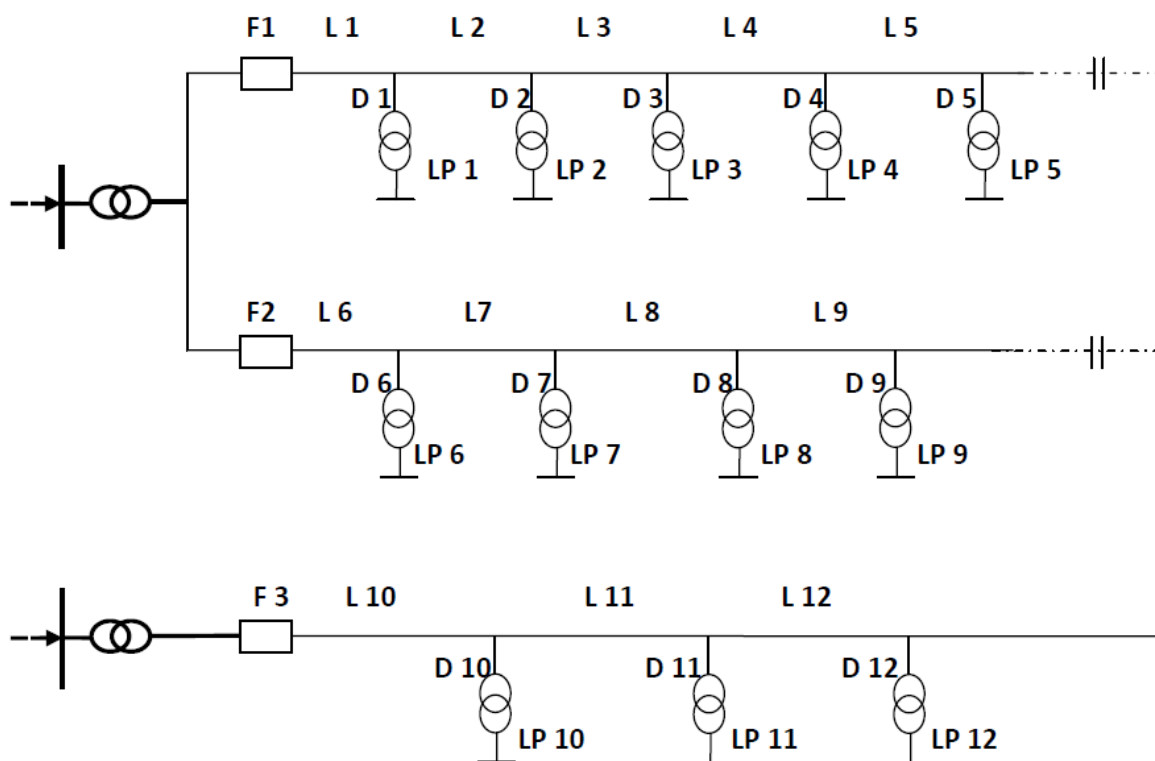


Fig.1: Three feeder distribution network

Input data

Table 1: Customer data

Load point	Customer type	Number of customer
LP1	Residential	1000
LP2	Commercial	800
LP3	Residential	700
LP4	Residential	500
LP5	Commercial	450
LP6	Residential	800
LP7	Residential	550
LP8	Residential	430
LP9	Residential	600
LP10	Commercial	900
LP 11	Residential	100
LP12	Residential	400

Table 2: Line section length and failure rate

Feeder no. 1 data			Feeder no. 2 data			Feeder no. 3 data		
Enter line section length	in km length	Failure rate (in f/yr.)	Enter line section length	in km length	Failure rate (in f/yr.)	Enter line section length	in km length	Failure rate (in f/yr.)
L1	2	0.2	L6	4	0.4	L10	5	0.5
L2	1	0.1	L7	2	0.2	L11	7	0.7
L3	3	0.3	L8	4	0.4	L12	4	0.4
L4	2	0.2	L9	3	0.3	---	--	
L5	1	0.1	---	--		---	--	
D1	1	0.2	D6	3	0.6	D10	3	0.6
D2	3	0.6	D7	2	0.4	D11	4	0.8
D3	2	0.4	D8	4	0.8	D12	2	0.4
D4	1	0.2	D9	1	0.2	---	--	
D5	3	0.6	---	--		---	--	

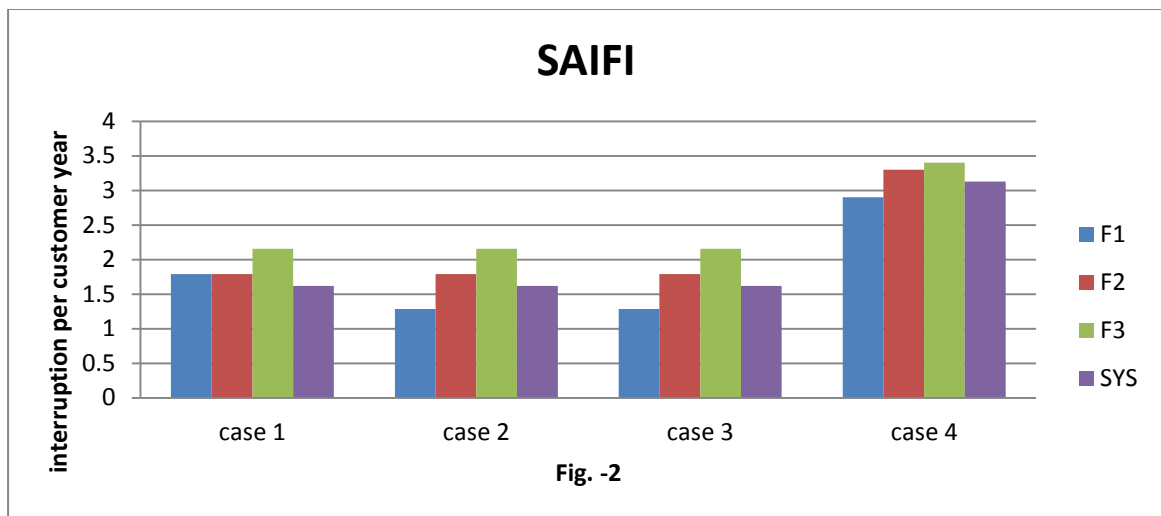
V. RESULT

The equipment failure rate and repair time are fuzzified by triangular membership function and minimum alpha cut are used in this work. The fuzzy expected failure rate and repair time are used to evaluate reliability indices and their corresponding credibility. The reliability indices evaluated for this study are System Average Interruption Frequency Index. System Average Interruption frequency index (SAIFI), System Average Interruption Duration Index (SAIDI), Customer Average Interruption Duration Index (CAIDI). The result obtained from the proposed method has been compared with the traditional methods Billinton et al (1996). A comparison of traditional method and proposed method the results obtained each three feeder for the four case studies are show in Table 3.

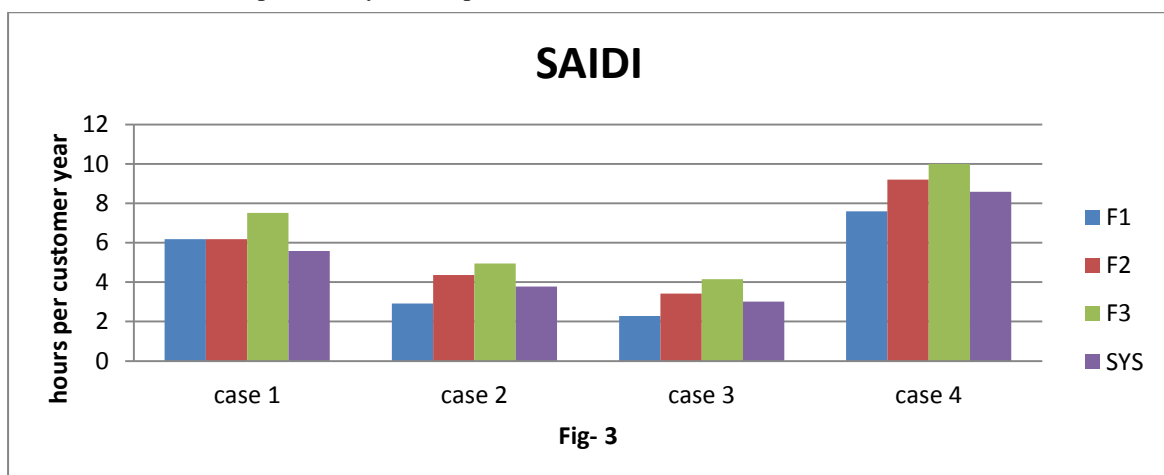
Table 3: Comparative Reliability Indices for Traditional Method and Proposed Method

	SAIFI	SAIFI	SAIDI	SAIDI	CAIDI	C AIDI
Case 1	Traditional method	Result obtain by proposed method	Traditional method	Result obtain by proposed method	Traditional method	Result obtain by proposed method
F1	1.7891	1.7152	6.1782	6.1144	3.4533	3.4089
F2	1.8831	1.80322	6.2732	6.21244	3.5633	3.51998
F3	2.1571	2.9422	7.5143	7.4672	3.4834	3.4398
SYS	1.6201	1.5858	5.5746	5.5387	3.441	3.4021
Case 2						
F1	1.2855	1.22978	2.9101	2.88233	2.2638	2.21787
F2	1.7891	1.74978	4.3634	4.32987	2.4389	2.393526
F3	2.1571	2.1366	4.9393	4.902321	2.2897	2.227998
SYS	1.6201	1.61433	3.7815	3.71868	2.3342	2.303885
Case 3						
F1	1.2855	1.216878	2.2832	2.2397	1.7761	1.72978
F2	1.7891	1.73879	3.4123	3.38786	1.9073	1.87325
F3	2.1571	2.11987	4.1443	4.128779	1.9212	1.89377
SYS	1.6201	1.597896	3.2152	3.18839	1.8612	1.836754
Case 4						
F1	2.9	2.87463	7.6	7.57021	2.6207	2.596732
F2	3.3	3.25987	9.2	9.17023	2.7879	2.722787
F3	3.4	3.36997	10	9.9783	2.9412	2.877357
SYS	3.1285	3.0993789	8.5914	8.547862	2.7462	2.717649

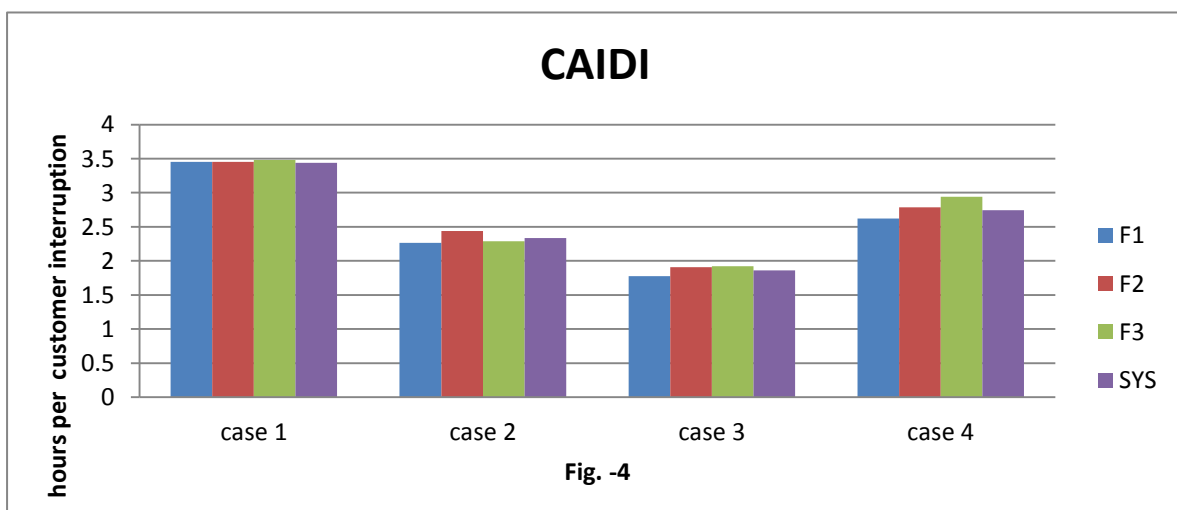
In our approach equipment failure and repair time are uncertain, so reliability indices will also not assured. Thus credibility also a good in addition to fuzzy expected of reliability indices. The credibility is evaluated for eight cases of each distribution system reliability indices. The result obtained by this technique is shown in Fig. 2 to Fig. 4.



The system average interruption frequency index (SAIFI) is commonly used as a reliability indicator by electric power utilities. In Fig. - 2 show that a customer would experience minimum SAIFI in case-2 & case-3 and maximum in case-4. This means that case-3 is more reliable than case-4 because customer connected to system as case-2 & case-3 would experience lesser no of interruption in a year compared to other cases.



The system average interruption duration index (SAIDI) is also commonly used as a reliability indicator by electric power utilities. In Fig. - 3 show that a customer would experience minimum SAIDI in case-3 and maximum in case-4. This means that in case-3 average outage duration is less in out of all four cases. And SAIDI maximum in case-4 means outage duration for each customer served is less duration than other cases.



The customer average interruption duration index (CAIDI) is gives the average outage duration that any given customer would experience. CAIDI can also be viewed as the average restoration time. In Fig-4 shows that a customer would experience minimum CAIDI in case-3 and maximum in case-1. The customer of case-3 would experience minimum average restoration time/outage duration then other cases.

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